FIRST ORDER ALLPASS FILTERS EMPLOYING A SINGLE INVERTING SECOND GENERATION CURRENT CONVEYOR WITH AN APPLICATION EXAMPLE

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Abstract: A configuration containing a single inverting second generation current conveyor (ICCII) is presented. It realizes six different voltage mode first order allpass filters. As the application example, an oscillator circuit that uses one of these ICCII based filters is given. The theoretical analysis is verified by PSPICE simulations using a CMOS realization of ICCII. Experimental results are also included.

Keywords: Analog signal processing, first order allpass filter, inverting second generation current conveyor (ICCII), quadrature oscillator.

1. Introduction

Allpass filters are important parts of many electronic circuits and systems. They are generally used for introducing a frequency dependent delay while keeping the amplitude of the input signal constant over the desired frequency range [1, 2]. Other types of active circuits such as quadrature oscillators and high-Q bandpass filters are also realized by using allpass filters [1, 3]. Many first order allpass filter realizations using different active building blocks have been reported in the literature [2-4]. On the other hand, the inverting second generation current conveyor (ICCII) has been introduced as a new active element to give further possibilities to the analog designers [5]. Some ICCII based circuits are reported in the literature [5-10]. It has few applications to the realization of first order allpass filters [8-10]. In [8] four different voltage mode allpass filters have been presented. Chen, et al. has introduced an ICCII based configuration which provides both inverting and non-inverting first order allpass filtering functions simultaneously from the same topology [9]. First order allpass sections employing ICCIIs have been used for the synthesis of a current mode universal filter in [10]. None of these filters contain a grounded capacitor. In this paper, we present an ICCII based configuration which realizes six different first order allpass filters. All realizations are canonical since they include only one capacitor as a dynamical element. One of the presented filters employs a grounded capacitor. This filter has been used together with an ICCII based integrator, which also includes a grounded capacitor, to realize a quadrature oscillator. The functionality of the circuits has been shown by simulation and experimental results.

2. Circuit Description

The circuit symbol of ICCII element is shown in Figure 1. The port relations of the positive type ICCII are given by the following set of equations.

\[ I_x = 0 \]
\[ V_x = -V_y \]
\[ I_z = I_x \]

The configuration to be used in the synthesis of the first order allpass filters is given in Figure 2. Routine analysis of this configuration yields the following transfer function.

\[ \frac{V_{out}}{V_{in}} = -\frac{Y_x(Y_x + 2Y_z + Y_y) + Y_y(Y_x + 2Y_z - Y_y + 2Y_z)}{(Y_x + 2Y_z + Y_y)(Y_x + 2Y_z - Y_y + 2Y_z) + Y_y(Y_x + 2Y_z - Y_y + 2Y_z)} \]

![Figure 1. Circuit symbol of ICCII](image-url)
Using various combinations for the admittances \((Y's)\), six different first order allpass filters can be obtained from this configuration as given in Table 1. The first two filters (circuits 1 and 2) correspond to the ones presented in [8]. Transfer function for the circuits 1-to-4 is

\[
T_1(s) = \frac{V_{out}}{V_{in}} = \frac{s - \frac{1}{RC}}{s + \frac{1}{RC}}
\]

and phase relation

\[
\phi_1(\omega) = 180^\circ - 2\arctan(\omega RC)
\]

The remaining two filters, i.e. circuits 5 and 6, have the following transfer function

\[
T_5(s) = \frac{V_{out}}{V_{in}} = -\frac{s - \frac{1}{RC}}{s + \frac{1}{RC}}
\]

and phase relation

\[
\phi_2(\omega) = -2\arctan(\omega RC)
\]

Therefore, both inverting and non-inverting types of first order allpass filters can be realized with the configuration of Figure 2. The only one that contains a grounded capacitor is the circuit 5 in Table 1.

If we also take into account the non-idealities of ICCII (i.e. \(I_Y=0, V_X=\beta V_Y, I_Z=\alpha I_Z\)) for circuit 5, its transfer function becomes

\[
T_4(s) = \frac{V_{out}}{V_{in}} = -\frac{s - \frac{1}{RC}}{s + \frac{1}{\alpha\beta RC}}
\]

As it is evident from Equation (7), the non-idealities have the same effect both on numerator and denominator, and hence they will not deteriorate the allpass filtering function of the circuit 5. Only the characteristic frequency and thus the phase relation will change as below

\[
\phi_5(\omega) = -2\arctan(\omega \alpha \beta RC)
\]

The values of resistor and capacitor can be modified as \(R/\alpha\) and \(C/\beta\) in order to eliminate the effect of non-idealities completely.

### Table 1. Admittance combinations for the realization of the first order allpass filters

<table>
<thead>
<tr>
<th>Circuit No</th>
<th>(Y_1)</th>
<th>(Y_2)</th>
<th>(Y_3)</th>
<th>(Y_4)</th>
<th>(Y_5)</th>
<th>(Y_6)</th>
<th>(Y_7)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>(sC)</td>
<td>(1/R)</td>
<td>0</td>
<td>(\infty)</td>
<td>0</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>2</td>
<td>(\infty)</td>
<td>0</td>
<td>0</td>
<td>(sC)</td>
<td>0</td>
<td>(1/(2R))</td>
<td>0</td>
</tr>
<tr>
<td>3</td>
<td>(\infty)</td>
<td>0</td>
<td>0</td>
<td>(sC)</td>
<td>(1/R)</td>
<td>0</td>
<td>(1/R)</td>
</tr>
<tr>
<td>4</td>
<td>(\infty)</td>
<td>(1/(2R))</td>
<td>0</td>
<td>(sC)</td>
<td>0</td>
<td>0</td>
<td>(1/R)</td>
</tr>
<tr>
<td>5</td>
<td>(1/R)</td>
<td>0</td>
<td>0</td>
<td>(1/R)</td>
<td>(sC)</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>6</td>
<td>(2/R)</td>
<td>0</td>
<td>(sC/2)</td>
<td>(1/R)</td>
<td>0</td>
<td>0</td>
<td>0</td>
</tr>
</tbody>
</table>
3. Quadrature Oscillator As The Application Example

It is a well-known fact that a sinusoidal quadrature oscillator can be realized using an allpass section and an integrator [11] as shown in Figure 3. Using this block diagram, ICCII based quadrature oscillator can be implemented. To this end, the presented first order allpass filter and an ICCII based integrator, which can be realized by the circuit of Figure 4, are used together with voltage buffers for cascade connection. For providing a sinusoidal oscillation, the loop gain of the circuit is set to unity at \( s = j\omega \), i.e.

\[
\left[ \frac{s - 1/(R_iC_i)}{s + 1/(R_iC_i)} \right] - \frac{1}{sR_iC_2} = 1
\]  

(9)

From Equation (9) oscillation condition and frequency can be found respectively as

\[
R_iC_i = R_iC_2
\]  

(10)

\[
\omega_0 = \frac{1}{\sqrt{R_iC_iR_iC_2}}
\]  

(11)

For simplicity, if we choose \( R_i = R_j = R \) and \( C_1 = C_2 = C \), oscillation condition is satisfied and oscillation frequency becomes

\[
\omega_0 = \frac{1}{RC}
\]  

(12)

\[
\begin{array}{c}
\text{allpass section} \\
- s - 1/(R_iC_i) \\
\frac{s + 1/(R_iC_i)}{}
\end{array}
\quad
\begin{array}{c}
\text{integrator} \\
- \frac{1}{sR_iC_2} \\
V_1 \\
V_2
\end{array}
\]

Figure 3. Block diagram for quadrature oscillator

Figure 4. ICCII based integrator circuit

4. Simulation and Experimental Results

The first order allpass filter and the oscillator circuit have been simulated using PSPICE program. In the simulations, the CMOS realization of ICCII presented in [12] has been used together with 0.35\,\mu m CMOS process parameters. Supply voltages were taken as \( \pm 2.5\,V \). Simulated magnitude and phase responses of the first order allpass filter are shown in Figure 5. We used \( R=1\,k\Omega \) and \( C=100\,pF \) as the passive element values. Simulation results give the natural frequency as 1.58MHz, which is very close to the theoretical one (1.59MHz). Transient analysis of the filter has also been done using PSPICE simulations with the same passive element values. For this purpose, a sinusoidal voltage of 2V peak-to-peak with a frequency of 1MHz has been applied to the input of the filter and the output voltage has been observed. Figure 6 shows the simulated input and output voltages in time domain. According to the simulation results, there is 183ns of phase difference between the signals, which corresponds to 65.9 degrees. The theoretical value for the phase difference at 1MHz calculated using Equation (6) is 64.3 degrees, which is close to the simulated one. The distortion analysis has also been done. The total harmonic distortion at the output of the filter is found as 0.3% using PSPICE. The simulated output waveforms of the quadrature oscillator are shown in Figure 7 where all resistor and capacitor values were taken as 1k\,\Omega and 100\,pF, respectively. They oscillate at a frequency of 1.57MHz which is again near to the theoretical oscillation frequency (1.59MHz).

The circuits have also been tested experimentally. ICCII element has been implemented using Analog Devices’ AD844 integrated circuit as shown in Figure 8. Supply voltages were taken as \( \pm 5\,V \). Buffered output of the AD844 has been used for the cascade connection in the experimental setup of the quadrature oscillator. In the experiments, all resistor and capacitor values were taken as 1k\,\Omega and 10nF, respectively. Figure 9 shows the input (1V peak, 50kHz) and output waveforms of the first order allpass filter. As it is expected, the output waveform has been shifted by –145.5 degrees (theoretically –144.7 degrees) while keeping the amplitude almost unchanged. Figure 10 shows the experimental waveforms of the quadrature oscillator. They oscillate at a frequency of 16.3kHz (theoretical one is 15.9kHz) with 90 degrees phase difference between them.
Figure 5. Simulated magnitude and phase responses of the first order allpass filter

Figure 6. Transient response of the filter
5. Conclusions

An ICCII based configuration, which realizes six different first order allpass filtering functions, is presented. One of the filters is used together with an ICCII based integrator to form a quadrature oscillator as the application example of the presented filter. PSPICE simulation results verifying the predicted theory are included. The first order allpass filter and the quadrature oscillator circuits are also tested experimentally in the laboratory using the AD844 implementation of ICCII element.
6. References


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